Experimental Question 1: Levitation of Conductors in an Oscillating Magnetic Field
MARKING SCHEME

| a) 0.2 | Correct expression for $\epsilon$ | 0.1 | Disregard overall sign |
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|  | Correct expression for $I$ | 0.1 | Disregard overall sign |
| b) 0.6 | Understanding Gauss law for cylinder: $\Delta \Phi_{\mathrm{z}}=\Phi_{\mathrm{r}}$ | 0.3 |  |
|  | Writing $\Phi_{r}=2 \pi r \Delta z B_{r}$ | 0.1 |  |
|  | Result for $B_{r}$ | 0.2 | Disregard overall sign |
| c) 0.5 | Writing $F(t)$ correctly | 0.1 |  |
|  | Decomposing into sine-squared and sine-cosine products | 0.2 |  |
|  | Final answer | 0.2 |  |
| d) 1.3 | Reasonable circuit diagram for measuring current and voltage | 0.1 |  |
|  | Correct 4-terminal circuit diagram | 0.2 |  |
|  | Current and voltage measurements | 0.3 | At least 3 measurement sets -0.3 <br> 2 measurement sets -0.2 <br> 1 measurement set - 0.1 |
|  | Took into account that the measured voltage is not on the whole ring | 0.1 |  |
|  | Result for the resistance | 0.5 | Within $1.67 \mathrm{~m} \Omega-1.74 \mathrm{~m} \Omega-0.5$ Within $1.62 \mathrm{~m} \Omega-1.79 \mathrm{~m} \Omega-0.3$ Within $1.35 \mathrm{~m} \Omega-2.05 \mathrm{~m} \Omega-0.1$ |
|  | Error estimation | 0.1 |  |
| e) 1.3 | Measurement of closed ring's average diameter | 0.2 |  |
|  | Weighing the rings | 0.1 |  |
|  | Writing $R_{2} / R_{1}=\left(l_{2} / l_{1}\right)\left(A_{1} / A_{2}\right)$ | 0.1 |  |
|  | Writing $A_{1} / A_{2}=\left(l_{2} / l_{1}\right)\left(m_{1} / m_{2}\right)$ | 0.2 |  |
|  | Taking into account the gap in the open ring | 0.1 |  |
|  | Result | 0.4 | Within $0.150 \mathrm{~m} \Omega-0.160 \mathrm{~m} \Omega-0.4$ Within $0.145 \mathrm{~m} \Omega-0.165 \mathrm{~m} \Omega-0.2$ Within $0.120 \mathrm{~m} \Omega-0.190 \mathrm{~m} \Omega-0.1$ |
|  | Error estimation | 0.2 |  |
| f) 1.5 | Range of measured EMF | 0.3 | $\begin{aligned} & \text { At least } 5 \mathrm{mV}-20 \mathrm{mV}-0.3 \\ & \text { At least } 7 \mathrm{mV}-14 \mathrm{mV}-0.1 \end{aligned}$ |
|  | Number of measurement points | 0.3 | $\begin{aligned} & \hline \text { At least } 30 \text { points }-0.3 \\ & 20-29 \text { points }-0.1 \\ & \hline \end{aligned}$ |
|  | Calculating $z$ from number of turns | 0.2 | Either for each separate point or as a collective statement of units |
|  | Penalty for not writing correct units in the table | -0.1 |  |


|  | Graph of $\epsilon(z)$ | 0.7 | Reasonably smooth shape -0.2 <br> Using most of the paper area -0.2 <br> Error bars - 0.1 <br> Axes properly marked - 0.1 <br> Units - 0.1 |
| :---: | :---: | :---: | :---: |
| g) 1.0 | Range of measured force | 0.3 | $\begin{array}{\|l} \hline \text { At least } 0.3 \mathrm{gf}-5.5 \mathrm{gf}-0.3 \\ \text { At least } 0.6 \mathrm{gf}-3 \mathrm{gf}-0.1 \\ \hline \end{array}$ |
|  | Number of measurement points | 0.3 | $\begin{array}{\|l\|} \hline \text { At least } 30 \text { points }-0.3 \\ 20-29 \text { points }-0.1 \\ \hline \end{array}$ |
|  | Calculating $z$ from number of turns | 0.2 | Either for each separate point or as a collective statement of units |
|  | Subtracting the weight of the ring+block | 0.1 | Either with Tare option or manually |
|  | Errors | 0.1 |  |
|  | Penalty for not writing correct units | -0.1 |  |
| h) 1.4 | Finding the derivative $d \epsilon / d z$ or $d \epsilon^{2} / d z$ using differences between points on a smoothed graph | 1.1 | Drawing a smooth line on the graph (not exactly along the points) -0.2 <br> Finding the derivative from differences between points on the smooth line -0.5 <br> Using symmetric pairs of points for the derivative calculation - 0.2 <br> Using reasonable spacing of the pairs of points 0.2 |
|  | Finding the derivative of $d \epsilon / d z$ or $d \epsilon^{2} / d z$ using differences between measured points |  | Finding the derivative from differences between the measured points - 0.4 <br> Using symmetric pairs of points for the derivative calculation -0.2 <br> Using reasonable spacing of the pairs of points ( $6 \mathrm{~mm}-12 \mathrm{~mm}$ ) - 0.5 <br> (Partial credit for spacing of $4 \mathrm{~mm}-6 \mathrm{~mm}$ or 1215 mm - 0.2 ) |
|  | Finding the derivative by drawing tangents to the graph |  | Partial credit of 0.3 out of 1.1 for using this method. |
|  | Number of points where the derivative was found | 0.3 | $\begin{array}{\|l\|} \hline \text { At least } 15 \text { points }-0.3 \\ 10-14 \text { points }-0.1 \\ \hline \end{array}$ |
| i) 2.2 | Graph | 0.7 | Appropriate axes (e.g. $\langle F\rangle$ vs. $d \epsilon_{\text {rms }}^{2} / d t$ ), properly marked - 0.2 <br> Using most of the paper area -0.2 <br> Error bars - 0.2 <br> Units - 0.1 |
|  | Using a linear region for the slope | 0.2 |  |
|  | Finding the slope | 0.1 |  |
|  | Error of the slope | 0.1 |  |


|  | Expressing $L$ from the slope | 0.2 | Writing an equation for $L-0.1$ <br> Solving the equation (with correct root) -0.1 <br> Partial credit for neglecting $\omega L / R$ and a correct <br> calculation otherwise -0.1 |
| :--- | :--- | :--- | :--- |
|  | Result for $L$ | 0.7 | $0.110 \mu \mathrm{H}-0.121 \mu \mathrm{H}-0.7$ <br> $0.100 \mu \mathrm{H}-0.130 \mu \mathrm{H}-0.4$ <br> $0.090 \mu \mathrm{H}-0.140 \mu \mathrm{H}-0.1$ |
|  |  | 0.2 |  |
|  | Error calculation for $L$ |  |  |

